

**Not to hand in! For oral discussion in the exercise class on 11.10.2023**

Website: <http://reh.math.uni-duesseldorf.de/~khalupczok/krypto/>

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**Exercise 1:** Permutations in  $S_{26}$

How many  $\sigma \in S_{26}$  are there which

- (a) have order 2 (i. e.  $\sigma(\sigma(n)) = n$  for all  $1 \leq n \leq 26$ ),
- (b) have at most  $k$  many fix points ( $1 \leq n \leq 26$  with  $\sigma(n) = n$ ),
- (c) contain no cycle of length  $> 13$ ?

**Exercise 2:** Paper-Enigma

Construct the paper-Enigma from the website

<https://mckoss.com/posts/paper-enigma/paper-enigma.pdf>

- (a) Encrypt with it (choosing the given adjustment I-II-III: MCK of the rotors) the plain text “INVOLUTION”
- (b) Which of the three plain texts can not be the beginning of the generated secret text GBDQQBHNWZTA... (from the Enigma in (a)), and why not? WETTERBERICHT, OBERKOMMANDO, KEINEBESONDERENVORKOMMNISSE

**Exercise 3:** Mini-Enigma

Given an Enigma with alphabet  $\sigma = \{A, E, H, N\}$ , two rotors and one Reflector. A plain text is known to be “AHNEHANNAHNAHEANNE”, which has been encrypted to “HAENAHEE-HAEHANHEEN”.

- (a) Give the secret text which is generated by the Enigma (in the same adjustment) for the plain text “NAEHEANNA”.
- (b) Give a possible “inner wiring” of the rotors, such that this encryption can be reached by the Enigma.